## Janitor

## Input File: janitorin.txt <br> Output File: janitorout.txt

Congratulations! You have been appointed head bathroom janitor of your school! Okay, okay, I know you're not thrilled, but somebody has to do it. We thank you for your sacrifice.

The bathroom floor is covered in a rectangular grid of tiles. No one is watching you very closely, so pouring a bucket of water over the floor is enough to make it look like you cleaned it. There is one small problem. The floor is uneven, so depending on which tile you pour the water on, some tiles may not become wet at all, and your deception will be exposed.

Water can flow from any square to any adjacent square of lower height, where adjacent squares may be to the north, south, east or west (water cannot flow across diagonals).

To finish your chore as soon as possible, you've decided to find out what is the fewest number of tiles you need to pour water on to make sure every tile becomes wet.

To complicate matters further, the bathroom is undergoing some hasty renovations. Each day, a tradie will replace one of the tiles, changing its height. After each replacement, you will need to figure out again how many tiles you need to pour water on.

## Input

- The first line of input contains three space-separated integers, $R, C$, and $Q$. There are $R$ rows and $C$ columns of tiles and there will be $Q$ replacements made by the tradies.
- The next $R$ lines each contain $C$ space-separated integers, giving the initial heights of the tiles. The tradie did such a terrible job at tiling the bathroom that literally no two adjacent tiles have the same height, even after any replacements.
- The following $Q$ lines each contain three integers $r_{i}, c_{i}$ and $h_{i}$. This indicates that the tradies have replaced the tile situated in row $r_{i}$ and column $c_{i}$ with a tile of height $h_{i}$. Rows are labelled from 1 to $R$ (from top to bottom) and columns are labelled from 1 to $C$ (from left to right).


## Output

The output should contain $Q+1$ lines. The first line should contain the fewest tiles you need to pour water on to make sure every tile gets wet before any replacements are made. The next $Q$ lines should correspond to the $Q$ tile replacements. After each replacement has been made (including all previous modifications), your program should write one line containing the fewest tiles you need to pour water on to make sure every tile gets wet.

## Sample Input

343
5320
4843
5761
231
$\begin{array}{ll}3 & 1 \\ 2\end{array}$
239

## Explanation

## Sample Output

2
3
3
2

Before first replacement

After second replacement



After first replacement


After third replacement

Initially, you need to pour water on the tile of height 5 and the tile of height 8. From there, the water will spread to the rest of the tiles. You can't cover the entire floor by pouring on one tile, so the answer is 2 .

After the first replacement, you need to additionally pour water on the tile in the 2nd row, 4th column (which has height 3). Now the answer is 3 .

After the second replacement, pouring on the same three tiles is still the best you can do.
After the last replacement, you can cover the floor by pouring on the height 5 tile and the newly added height 9 tile. The answer is 2 again.

## Subtasks \& Constraints

For all subtasks:

- $1 \leq R \leq 10$.
- $1 \leq C \leq 100000$.
- $1 \leq Q \leq 100000$.
- Each tile's height will always be between 0 and 1000000 inclusive.
- No two adjacent tiles will have the same height.

Subtasks:

- For Subtask 1 (10 points), $R, C \leq 3$ and $Q=1$.
- For Subtask 2 ( 25 points), $R=1$ and $Q \leq 1000$.
- For Subtask 3 ( 20 points), $R=1$.
- For Subtask 4 ( 25 points), $C, Q \leq 100$.
- For Subtask 5 (20 points), no further constraints apply.

